

### NeuroMathComp project team (INRIA, ENS Paris, UNSA LJAD)

# Modeling the Nature of Centre-Surround Interactions in Early Visual Cortex

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#### Introduction

- 1.1 Primary visual cortex V1
  1.2 Center-surround interaction
  Models and Methods
  2.1 Quantitative models
  2.2 Image decomposition
  Implementation results
  - 3.1 Optimization
  - 3.2 Further discussion



#### Primary Visual Cortex V1



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#### Primary Visual Cortex V1

Neurons in V1 orientations, spatial frequencies, colors....

#### Simple cells

bars of light, line orientated, center-on/off

#### Complex cells line orientation, excitatory/ inhibitory zone

Hyper Complex Cells moving corners or angles

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#### Primary Visual Cortex V1



#### **Drifting oriented luminance spots**

V1 NEURONS spatial frequency, orientation selectivities (1st), motion, direction, speed.....

code local contrast





## Simultaneous Contrast





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# one aspect Orientation tuning

Schwartz and Simoncelli, 2001





#### Surround suppression is locally anisotropic Schwartz & Simoncelli, 2001 Modeling surrond suppression in V1 neurons with a statistically-derived normalization model



#### Surround suppression should be locally isotropic Petrov and McKee (2006) The effect of spatial configuration on surround suppression of contrast sensitivity

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#### **Quantitative Models**



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#### **Normalization Model**



# cortical channels interaction

overlap,

orientation channel

spatial frequency channels

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#### **Normalization Model**





#### **Normalization Model**



- Nonlinearity of contrast response function
- Inhibition from neighbor stimulus
- Mathematical simplicity
- Code more efficiently



High neighbor contrast & low center contrast Asymptotic inhibition, Ejima & Takahashi (1985)

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#### **Multiplicative Model**





#### **Multiplicative Model**

$$R = \frac{AC_t^{\alpha}}{\sigma^{\beta} + C_t^{\beta}} \left(1 + \frac{B}{1 + \left(\frac{qC_n}{C_t}\right)^{\gamma}}\right) \quad (2)$$



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#### **Multiplicative Model**



- Nonlinearity of contrast response function
- Amplify the spatial interaction
- The saturation of spatial interaction



• Two more parameters

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#### Image Decomposition





#### **Gabor Filter**

$$g(x, y, \lambda, \theta, \phi, \sigma, \nu) = \exp(-\frac{x'^2 + \nu y'^2}{2\sigma^2})\cos(2\pi \frac{x'}{\lambda} + \phi) \quad (3)$$

$$x' = x\cos(\theta) + y\sin(\theta), \quad y' = -x\sin(\theta) + y\cos(\theta)$$

$$\lambda: \text{wavelength}, \quad \theta: \text{orientation}, \quad \phi: \text{phase offset}, \quad \sigma: \text{Gaussian envelope}$$

$$\text{orientated kernel} \quad \bullet \quad \text{direction selectivity}$$







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### **Gabor Filter**







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The Steerable Pyramid

Linear



*— Multi-orientation* 

# Directional derivative operator

order *orientations* 

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#### The Steerable Pyramid



- No orthogonality
- Rotation invariant
   Orientation
- Translation invariant
   Position
- Independent scale
- Independent orientation



Over-completeness 4/3K

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## The steerable pyramid

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## The Steerable Pyramid



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- 3.1 Optimization
- 3.2 Further discussion

#### **Implementation Results**





#### **Objective function**



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## The wavelet pyramid

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## **Extracting channels**



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#### **Optimization algorithm**

$$\{\hat{\omega}, \hat{\sigma}\} = \arg\min \mathbf{E} [C^2 - \sum \omega_k P_k^2 - \sigma^2]^2$$

Extract the corresponding coefficients matrix,  $128 \times 128$ 

Choose a  $13 \times 13$  window with the center pixel modeling the center neuron

Link  $\{\omega_k\}$  to each pixel in this window

Move the window over the whole extracted area to establish the objective function

Apply optimization algorithm to find the weights  $\{\omega_k\}$  by minimizing the objective function

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#### Conclusion and further discussion



### Optimized weights



#### Conclusion and further discussion

• Symmetric

Directional

Declining
 Surround suppression is locally anisotropic
 Schwartz & Simoncelli, 2001

#### Surround suppression should be locally isotropic Petrov and McKee (2006)



### Petrov & McKee (2006)'s experiment





Surround layout around the target

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### Conclusion and further discussion



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INSTITUT NATIONAL DE RECHERCHE EN INFORMATIQUE ET EN AUTOMATIQUE Conclusion and further discussion



Surround suppression is locally anisotropic Schwartz & Simoncelli, 2001

Further:

Across scales, optimization principle...

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# Thank you for your attention!

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